

<b>Using congruent triangles</b>	Season	01
	Episode	AP10
	Time frame	1 period

**Prerequisites :** Vocabulary and notions about triangles and angles.

**Objectives :**

- Use congruent triangles to solve problems.

**Materials :**

- *Exercises.*

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## 1 – Exercises

Whole period

Working by pairs, students have to solve some exercises and hand out a paper to the teacher at the end of the period.

## Exercise 1

Let  $ABC$  be a scalene triangle, with  $CDFG$  and  $ABDE$  two squares built outside of it

1. Decompose the angles to prove that  $\angle CBD = \angle ABF$ .
2. Deduce that  $\triangle BCD$  and  $\triangle ABF$  are congruent.
3. Deduce that  $AF = DC$ .

## Exercise 2

Let  $d_1$  and  $d_2$  be two parallel lines, with  $A$  a point on  $d_1$  and  $B$  a point on  $d_2$ . Let  $K$  be the midpoint of the segment  $AB$ . Through  $K$ , draw a line ( $\mathcal{D}$ ) that intersects  $d_1$  in  $M$  and  $d_2$  in  $N$ .

1. Prove that the triangles  $KAM$  and  $KBN$  are congruent.
2. Deduce the position of  $K$  on  $MN$ .

## Exercise 3

Let  $ABC$  be a scalene triangle, with  $I$  the midpoint of  $BC$ . Let  $B'$  and  $C'$  be the orthogonal projections of  $B$  and  $C$  onto the median  $AI$  of the triangle.

1. Prove that the triangles  $IBB'$  and  $ICC'$  are congruent.
2. Deduce from the previous question the nature of  $BBCC'$ .

## Exercise 4

Let  $ABCD$  be a square with center  $O$  and  $M$  a point on the side  $AB$ . Let  $P$  be the intersection of the side  $AD$  and the line perpendicular to  $CM$  through  $B$ .

1. Prove that  $\angle DCM = \angle BMC$  and deduce that  $\angle BCM = \angle ABP$ .
2. Deduce that the triangles  $MCB$  and  $PBA$  are congruent and that  $MB = AP$ .
3. Prove that the triangles  $OMB$  and  $OPA$  are congruent.
4. Deduce that  $\triangle POM$  is right-angled and isosceles.