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| Vectors and configurations | Season | 01 |
| | Episode | 14 |
| | Time frame | 1 period |

Prerequisites : Basic notions about vectors.

Objectives :

- Discover some simple but important configurations involving vectors.
- Practise the vocabulary about geometry.

Materials :

- *Hand-outs with all the configurations and properties.*
- *Properties involving vectors and figures.*

1 – Matching game

10 mins

Each student is handed out a card with either a property involving vectors or a figure. Students mingle to find who has the right property for their figure and vice-versa.

2 – Writing a property

15 mins

Each pair has to write a precise rule about the property and figure they have. The teacher checks each one of them.

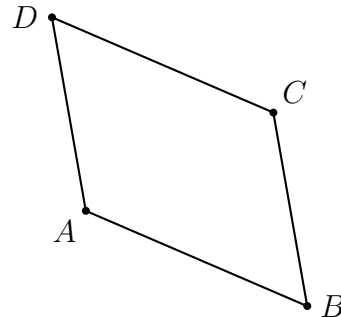
3 – Presentations

30 mins

Each pair goes to the board to explain their property. A hand-out with all properties is given at the end of the session.

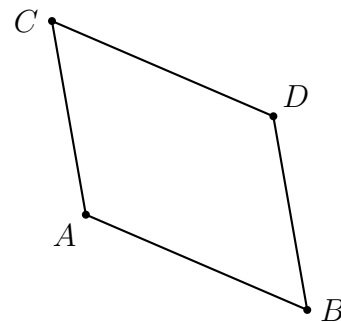
A quadrilateral $ABCD$ is a parallelogram if and only if

$$\overrightarrow{AB} = \overrightarrow{DC}.$$



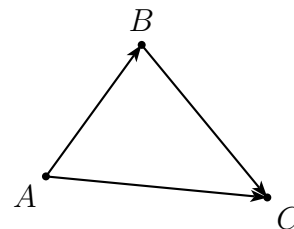
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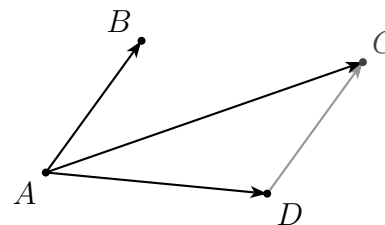
For any three points A , B and C ,

$$\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC}.$$



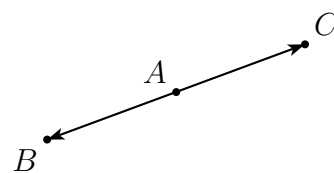
A quadrilateral $ABCD$ is a parallelogram if and only if

$$\overrightarrow{AB} + \overrightarrow{AD} = \overrightarrow{AC}.$$



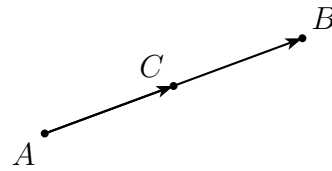
A point A is the midpoint of a segment BC if and only if

$$\overrightarrow{AB} + \overrightarrow{AC} = \vec{0}.$$



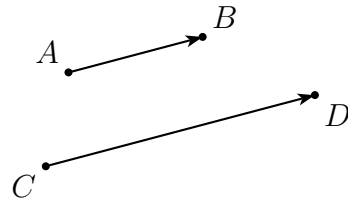
A point C is the midpoint of a segment AB if and only if

$$\overrightarrow{AB} = 2\overrightarrow{AC}.$$



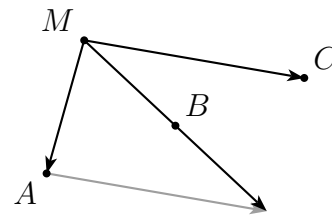
The fact that the lines CD and AB are parallel, that the vectors have the same direction and that $CD = 2AB$ can be written as the equality

$$\overrightarrow{CD} = 2\overrightarrow{AB}.$$



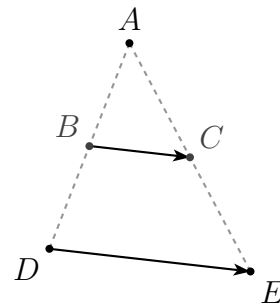
If point B is the midpoint of a segment AC , then for any point M ,

$$\overrightarrow{MA} + \overrightarrow{MC} = 2\overrightarrow{MB}.$$



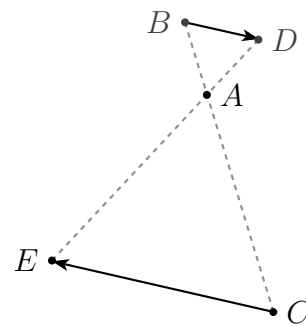
If the points B and C are the midpoints of the legs of a triangle ADE , then

$$\overrightarrow{DE} = 2\overrightarrow{BC}.$$



If A is the intersection of two segments BC and DE such that $AB = \frac{1}{3}AC$ and $AD = \frac{1}{3}AE$ then

$$\overrightarrow{BD} = -\frac{1}{3}\overrightarrow{CE}.$$



Document 1 Properties and figures

| | |
|---|--|
| $\overrightarrow{AB} = \overrightarrow{DC}$ | $\overrightarrow{AB} = \overrightarrow{CD}$ |
| $\overrightarrow{AB} + \overrightarrow{BC} = \overrightarrow{AC}$ | $\overrightarrow{AB} + \overrightarrow{AD} = \overrightarrow{AC}$ |
| $\overrightarrow{AB} + \overrightarrow{AC} = \vec{0}$ | $\overrightarrow{AB} = 2\overrightarrow{AC}$ |
| $\overrightarrow{CD} = 2\overrightarrow{AB}$ | $\overrightarrow{MA} + \overrightarrow{MC} = 2\overrightarrow{MB}$ |
| $\overrightarrow{DE} = 2\overrightarrow{BC}$ | $\overrightarrow{BD} = -\frac{1}{3}\overrightarrow{CE}$ |

